THE EVALUATION OF NIST-7: A NEW ERA

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Abstract

We have developed a set of evaluation tools whereby <u>all</u> of the known systematic effects are evaluated by means of leveraged experiments not involving, or limited by, precision frequency measurements. This both speeds the evaluation process and greatly reduces the "combined standard uncertainty," extending the operational life of thermal-beam technology.

I. Introduction

In traditional evaluations of primary, cesiumbeam frequency standards, the comparatively large frequency bias from the second-order Zeeman effect is evaluated in a highly leveraged way by measuring first order Zeeman splittings. Similarly, the second order Doppler effect is evaluated by measuring the atomic However, the accepted technique for evaluating many small (often zero) frequency bias terms has been to observe the parametric dependence of the frequency on some operating parameter. Examples are the magnetic field inhomogeneity, line overlap shifts and various imperfections in the electronics. Painfully long, precision frequency measurements are made which, at best, return information about the potential bias limited by the frequency measurement precision. information of this type is combined to give an overall estimate of the accuracy of the standard (1) many of the terms are of comparable size and (2) there are difficult questions about correlated terms. This both limits the attainable overall accuracy and leads to serious concern about how the many uncertainty terms should be combined: arithmetic sum or square root of the sum of the squares (RSS)? We have developed a set of evaluation tools that allow all the systematic effects we know to be evaluated in leveraged experiments that do not involve, and are not limited by, precision frequency Knowledge of the values and measurements. independence of the various bias terms is vastly improved.

II. Traditional Evaluation

When evaluating a standard, we make frequency difference measurements between the standard and a reference clock. We choose to represent these

measurements as

$$F = v_{cs} - v_{r} \pm \sigma + \sum b_{i} ,$$

where F is the measured frequency, v_{cs} is the frequency of the *unperturbed* cesium hyperfine resonance, v_r is the frequency of the reference clock, σ is the uncertainty in the frequency measurement imposed by the averaged measurement noise, and Σ b_i is the sum over all frequency biases. Implicit in this representation are that v_r is constant over the measurement period (hours to days to weeks), and the list of systematic effects is complete and includes any individual variation (environmental effects) and their associated uncertainty; that is, each b_i is, in fact, b_i(t, σ_i).

From this representation, it is easy to see the problems and limits to an evaluation based, even in part, on measurements involving the parametric dependence of the frequency on some operating parameter like microwave power or C-field. First, the bias of interest may not vary strongly with the clock operating parameter. Second, many other biases may also change with the same operating parameter. And, finally, all of the measurements are limited by σ , the frequency measurement precision. This not only seriously limits the uncertainty with which bias effects studied by this technique can be evaluated. It also leads to limited knowledge about correlations between uncertainties of different bias effects and, hence, questions about how best to combine uncertainties in the final, overall error budget, that is, arithmetic sum or RSS.

III. New Evaluation Tools

We now evaluate the smaller physical biases through a number of leveraged techniques. Shifts resulting from the magnetic field inhomogeneity, cavity pulling and overlap of neighboring Zeeman lines are evaluated by measuring the offset of each Ramsey fringe from its corresponding Rabi pedestal as a function of Zeeman state (m_F), microwave power and C-field value.² Fluorescence light shift can be quantitatively amplified by changing the optical pumping transition and geometry. Similarly, distributed-cavity phase shift can be forced quantitatively by movable beam masks placed in front of the cavity beam windows. Microwave leakage outside the standard and its routes into the

standard are hunted down and stopped.³ Leakage within the standard is accounted for in the beam reversal only if it remains constant in phase and amplitude every place within the standard during the evaluation. We have injected radiation into the standard to study these effects, and have taken pains in the design and operation of the standard to insure this effect is under control.

Imperfections in the electronics can result in shifts to the apparent, as-measured line position. RF spectral purity and some problems associated with switching transients have been published elsewhere.4 Many of the potential effects (modulation asymmetry or feedthrough into the signal channel, synchronous AM on the laser or the RF, for example) can be studied by interrupting the servo loop at some point and observing the integrator output over time. Pure noise will result in a random walk while a coherent, systematic effect will accumulate linearly. One has to average long enough to see the linear drift above the integrated noise. The leverage in this type of measurement comes from the fact that one can usually configure the standard to reduce the equivalent noise into the integrator during the test; e.g., block the atomic signal while looking for integrator offset or reference signal cross-talk, block the optical pumping beam while looking for AM on the detecting laser. Of course, care must be taken to insure the effect under investigation is not altered and nonlinear or digital aliasing are properly treated.

In this way, we are able to measure (or calculate) every bias we know (except end-to-end phase shift) with uncertainty small compared to our normal frequency measurement precision. Hence, their effects can be removed from the frequency measurement, producing a reduced frequency measurement f,

$$f = v_{cs} - v_{r} \pm \sigma + V\Phi ,$$

in which all of the otherwise known biases have been removed. Here, $V\Phi$ is the frequency bias resulting from the effective, end-to-end phase difference. We have separated the effective phase difference (Φ) from the velocity, microwave power, and modulation dependence (V) of the frequency shift. The value of V can be calculated using the data from the velocity measurements and known modulation parameters. The effective, end-to-end phase difference (Φ) is constant if microwave leakage and distributed-cavity, phase-shift have been properly handled. A pair of frequency measurements with beam reversal then yield

$$f = v_{cs} - v_{r} \pm \sigma + V\Phi$$

and

$$f' = v_{cs} - v_r \pm \sigma' - V'\Phi,$$

where the sign of the phase difference has reversed, the measurement precisions (σ) are of the same magnitude and the values of V differ slightly as a result of the different oven temperatures and beam alignments in the two directions. From these measurements, we can extract the effective, end-to-end, cavity phase shift with an uncertainty limited by that of the differenced frequency measurements:

$$\delta f = \pm \sqrt{\sigma^2 + {\sigma'}^2} + [V + V'] \Phi \simeq \pm \sqrt{2} \sigma + 2V \Phi.$$

However, if we combine the two frequency measurements in a weighted average, we get

$$\bar{f} = \frac{V/f + Vf'}{V + V'} \simeq v_{cs} - v_{r} \pm \frac{\sigma}{\sqrt{2}}$$
,

where the bias from end-to-end phase shift has dropped out *and* the individual measurements have combined to give a reduced net measurement noise. This result holds provided our initial conditions (v_r is constant, the set of b_i is complete, and their uncertainties are small compared to σ) are met. This process can also be extended to a larger set of frequency measurements to further average down the measurement noise.

IV. Results and Conclusions

This view of the evaluation process is new to us, and there remains a great deal of work to do to achieve the ultimate evaluation of NIST-7. However, a number of things are already clear. (1) In the list of potential systematic effects of which we are aware, it seems we can evaluate each of them with uncertainty below the present stability of our maser ensemble. (2) At the very least, the combined standard uncertainty of the ultimately evaluated standard will be greatly reduced from our originally estimated limit of 1×10^{-14} . (3) The fact that the noise type of individual frequency measurements is white, means that long runs are not necessary to lower measurement noise. frequency measurements can be combined with confidence. This allows more frequent looks at bias terms that may have environmental coupling. (4) There is a powerful internal diagnostic for the validity of #3 above: If N runs of individual precision σ do not combine to yield an overall statistical uncertainty of σ/\sqrt{N} , some bias is not under control.

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